

hands-on **problem solving** *A Minds-On Approach*

Grade 4

Senior Author

Jennifer Lawson

Writer

Dayna Quinn-LaFleche

Project Consultant

Dianne Soltess

Mathematics Consultants

Meagan Mutchmor, Manitoba

Tina Jagdeo, Ontario


Lara Jensen, Ontario



PORTAGE & MAIN PRESS

Winnipeg • Manitoba • Canada

© 2012 Jennifer Lawson

Pages of this publication designated as reproducible with the following icon  may be reproduced under licence from Access Copyright. All other pages may only be reproduced with the express written permission of Portage & Main Press, or as permitted by law.

All rights are otherwise reserved and no part of this publication may be reproduced, stored in a retrieval system, or transmitted in any form or by any means, electronic, mechanic, photocopying, scanning, recording or otherwise, except as specifically authorized.

Portage & Main Press gratefully acknowledges the financial support of the Province of Manitoba through the Department of Culture, Heritage, Tourism & Sport and the Manitoba Book Publishing Tax Credit, and the Government of Canada through the Canada Book Fund (CBF), for our publishing activities.

Hands-On Problem Solving, Grade 4

A Minds-On Approach

ISBN 978-1-55379-348-9

Printed and bound in Canada by Prolific Group

Editor:

Leslie Malkin

Book and Cover Design:

Relish New Brand Experience Inc.

Cover Photo Credits:

@iStockphoto.com

Illustrations:

Jess Dixon



PORTAGE & MAIN PRESS

100-318 McDermot Avenue

Winnipeg, MB, Canada R3A 0A2

Tel: 204-987-3500 • Toll free: 1-800-667-9673

Toll-free fax: 1-866-734-8477

Email: books@portageandmainpress.com

www.hands-on.ca

Contents

Introduction to Hands-On Problem Solving Grade 4

Program Introduction	
Program Principles	
Big Ideas in Mathematics	
Communication	
Connections	
Mental Math	
Estimation	
Reasoning	
Technology	
Visualization	
Problem Solving	
What Is Problem Solving?	
Best Practices in Teaching	
Problem Solving	
Routine Problems	
Non-Routine Problems	
Extended Exploration Problems	
Implementing the Hands-On	
Problem-Solving Program	
Program Format	
Planning Your Year of Problem Solving	
Curricular Connections	
Supporting Literacy During Problem Solving	
The Questioning Process	
Additional Resources	
A Note About Pennies	
Guiding and Supporting Learning –	
Problem Solving	
Mathematics Correlation	
Grade 4 Correlation Chart	

The Hands-On Problem Solving Assessment Plan

Assessment for Learning	
Assessment as Learning	
Assessment of Learning	
Performance Assessment	
Portfolios	
Assessment Blackline Masters	

Routine Problems

1	Implementation of Routine Problems	25
2	Problem Types	26
2	Teaching Routine Problems	27
2	1A Mad About Marbles	32
2	2A Gathering Acorns	35
3	3A Reading Challenge	38
3	4A The Largest Number	41
3	5A Taking Goats to the Fair	44
4	6A How Tall Is Spencer?	46
4	7A Pumpkin Seed Project	48
4	8A How Much TV?	50
4	9A A Box of Chocolates	53
4	10A How Much Money Is Left?	55
	11A Miranda's Shadow	57
5	12A Collecting Cans of Soup	59
5	13A A Driving Holiday	61
5	14A The Shortest Living Man	63
7	15A Practising Piano	65
	16A Mailing Letters	67
7	17A How Many Kilometres?	70
7	18A Summer Camp Supplies	72
7	19A Hoping to See the Concert	74
8	20A Eating Pizza	76
	21A Buying Gum	78
8	22A Balls for the Golf Tournament	80
8	23A Stick-on Tattoos	82
8	24A Herding the Sheep	84
8	25A Discussing...Diapers?	86
	26A Mathematics With Vowels and Consonants	88
10	27A Beads for Plaster Art	90
11	28A The Wild Monkey Roller Coaster	92
	29A The Terry Fox Run Lemonade Fundraiser	94
13	30A T-Shirt Survey	96
13	31A Toothpick Shapes	98
14	32A Drawing 2-D Shapes	100
14	33A A Symmetrical Design	102
14	34A Building 3-D Skeletons	104
16	35A A Castle of 3-D Solids	106

36A Running Late	108	26B How Many Cans of Paint?	192
37A The Dog Run	111	27B Numbers on Lockers	194
38A Estimating Time	113	28B Pizza for Charity	196
39A Not Keeping Time	115	29B Megan Makes a Math Mobile	198
40A A Long Bus Trip	117	30B How Old Will Chico Be?	200
Non-Routine Problems	119	31B Saving for a Bike	202
Implementation of Non-Routine Problems	120	32B Seven Layer Salad	205
Teaching Non-Routine Problems	123	33B Half of Half of Half...	207
An Additional Resource for Solving Non-Routine Problems	125	34B How Many Girls and Boys?	209
Guiding and Supporting Learning – Non-Routine Problems	126	35B In What Order Are the Shapes?	211
1B Silas's Cap Collection	127	36B Hexagon Sandboxes	213
2B Building Numbers With Base-Ten Blocks	131	37B Singles and Doubles Badminton	215
3B Number Sentences	133	38B Building a Patio	217
4B Climbing Up the Well	135	39B Spruce Up the School Day	219
5B Putting Away the Balls	137	40B Toothpick Houses	221
6B Putting the Cake Orders Back in Sequence	139	Extended Exploration Problems	223
7B Collecting Fossils	143	Implementation of Extended Exploration Problems	224
8B Building a Pyramid Model	146	Teaching Extended Exploration Problems	224
9B Geese Flying South	149	Guiding and Supporting Learning – Extended Exploration Problems	228
10B How Many Marbles in Each Container?	152	1C Number Architect	229
11B Who Scored That Touchdown?	154	2C A Game That Lasts a Lifetime?	233
12B Considering Careers	156	3C Curling Challenge	235
13B The Archery Tournament	159	4C Designing a Garden	238
14B When Do the Children Rule the Schools?	162	5C Turkey Fundraiser	241
15B Six Pieces of Blue Shoelace Licorice	164	6C What Is Wrong With the Clock?	245
16B Feeding the Pets	167	7C Pattern Block Designs	248
17B Going to the Soccer Tournament	171	8C Planning a Car Trip	251
18B Wendy's Ice Cream Cart	174	9C Running Laps	254
19B Running Laps Around the Track	177	10C Planning a Feast	256
20B Making Stickers	179	Appendix	261
21B Building a Light-Rail Transit System	181	References	268
22B Perimeter of A Rectangle	183	About the Authors	269
23B Leftover Pizza	185		
24B Number Puzzler	187		
25B Placing Numbers on a Number Line	190		

Introduction to Hands-On Problem Solving Grade 4

Introduction to Hands-On Problem Solving Grade 4

Program Introduction

Hands-On Problem Solving focuses on developing students' knowledge, skills, attitudes, and strategic thinking related to mathematics through active inquiry, problem solving, and decision making. Throughout all activities presented in the book, students are encouraged to explore, investigate, and ask questions in order to heighten their own curiosity about and understanding of the world of mathematics.

Program Principles

1. Effective problem-solving programs involve students actively building new knowledge from experience and prior knowledge.
2. Development of students' understanding of concepts, flexibility in thinking, reasoning, and problem-solving skills/strategies form the foundation of the problem-solving program.
3. From a young age, children are interested in mathematical ideas. This interest must be maintained, fostered, and enhanced through active learning.
4. Problem-solving activities must be worthwhile and relate to real-life experiences. Problems should be rooted in context so that students can make sense of the numbers with which they are being asked to work in a meaningful way.
5. The teacher's role in the problem-solving process is to actively engage students in tasks and experiences designed to deepen and connect their knowledge. Children learn best by doing, rather than by just listening. The teacher, therefore, should focus on creating opportunities for students to interact in order to propose mathematical ideas and conjectures, to evaluate their own

thinking and that of others, and to develop mathematical problem-solving skills.

6. Problem solving should be taught in correlation with the mathematics program and with other school subjects. Themes and topics of study in problem solving should integrate ideas and skills from mathematics, as well as from other areas of study, whenever possible.
7. The problem-solving program should encompass and draw on a range of educational resources including literature and technology as well as people and places in the local community.
8. Assessment of student learning in problem solving should be designed to focus on performance and understanding and should be conducted through meaningful and varied assessment techniques carried on throughout the modules of study.

Big Ideas in Mathematics

In order to achieve the goals of mathematics education and to support lifelong learning in mathematics, students must be provided with opportunities to encounter and practise critical mathematical processes. Problem solving is one of these processes, but since they are all inter-related, it is important to recognize the characteristics of each mathematical process, and the related learning experiences for students. These processes are as follows:

Communication

Students need opportunities to share their mathematical ideas and thinking through oral language, reading and writing, diagrams, charts, tables, and illustrations. Communicating mathematically, aloud or on paper, helps students clarify their thinking for themselves and others.

For example:

There are 12 goldfish.

The goldfish are in fishbowls.

Each bowl has the same number of goldfish in it.

Show different ways the goldfish could be put into fishbowls.



Connections

When doing problem-solving activities in the classroom, teachers should ensure that links are made between the various strands of the mathematics curriculum. It is also important to make connections between concrete, pictorial, and symbolic representations, so students should be encouraged to explore the use of manipulatives, illustrations, and symbols to solve problems. Further, concepts and skills should be connected to everyday life and to other curricular areas.

Mental Math

Mental math is more than just knowing the facts—it is about strategic thinking and number sense. Mental math is a process necessary to many everyday experiences, and students need extensive exposure to activities that encourage them to solve problems mentally. Strong mental math skills enable students to respond quickly to

questions or required tasks phrased in a variety of ways. For example:

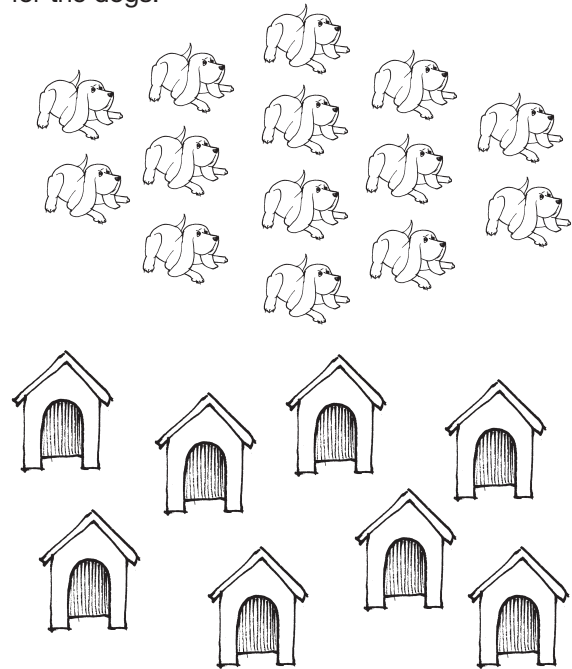
- Double 7
- Half of 12
- Two 6s
- You roll double 3. What's your score?
- How many shoes in 9 pairs?

Estimation

Students should be encouraged regularly to estimate quantities and measurements. Being able to make an educated guess allows students to independently check the validity of their calculations. It is also an essential skill in everyday life. Estimation encourages students to take risks, use background knowledge, and learn from the process.

For example:

Estimate whether there are enough dog houses for the dogs.



Now, check. Are there too many or too few dog houses?

Reasoning

Mathematical reasoning involves informal thinking, conjecturing, and validating. Students should be encouraged to justify their solutions, thinking processes, and hypotheses. Good reasoning is as important as finding correct answers, so students need many opportunities to think about, describe orally, and record their mathematical activities and ideas. For example:

I am a 2-digit number.

My tens digit is 2 greater than 3.

My ones digit is 3 less than my tens digit.

What number am I?

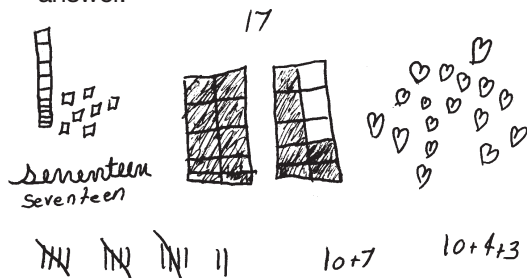
Technology

The use of calculators is recommended, to facilitate and enhance problem-solving skills and to encourage discovery of number patterns. However, calculators must not replace development of students' number concepts and skills. Other technologies such as interactive whiteboards, computer software, and websites can provide valuable resources for students and teachers as well.

Visualization

This is the process of creating mental images needed to develop concepts and understand procedures. Visualizations help students clarify their understanding of mathematical ideas. For example:

- Show all you know about the number 17. Use pictures, diagrams, and words in your answer.



Problem Solving

Problem solving is another of the “big ideas” in mathematics—the mathematical processes students need in order to achieve the goals of mathematics education and to support lifelong learning in mathematics. Students are exposed to a wide variety of problems in all areas of mathematics in ***Hands-On Problem Solving***. They also explore a variety of methods for solving and confirming their solutions to a variety of different types of problems. They should also be encouraged to find multiple solutions for problems and to create their own problems.

What Is Problem Solving?

Problem solving refers to “mathematical tasks that have the potential to provide intellectual challenges for enhancing students’ mathematical understanding and development” (Cai and Lester, NCTM). Problem solving is the application of a variety of mathematical knowledge, tools, and strategies to a wide range of math problems in order to solve them.

Problem solving

- Is a life skill;
- Creates a purpose for learning skills and concepts;
- Motivates students by developing a sense of inquiry;
- Allows students to demonstrate their understanding of mathematical concepts and skills in meaningful contexts;
- Teaches perseverance.

Problem solving should be the main focus of mathematics instruction. The ability to apply their knowledge to solve problems is the goal for all students.

Best Practices in Teaching Problem Solving

Problem solving is often not viewed positively by students. In order to change this perception teachers should

- Use a problem-solving approach when introducing and teaching concepts and skills;
- Begin with simple problems so students can experience success;
- Include a balance of routine, non-routine, and extended exploration problems;
- Encourage the use of multiple strategies for solving problems;
- Provide opportunities for students to write their own problems;
- Use modelling (think aloud) to demonstrate the thinking processes involved in solving a problem. Students will be reluctant to attempt a problem if they do not know where or how to begin.
- Provide time for reflection (journaling, summarizing, and so on) in order to clarify mathematical ideas and relationships;
- Encourage discussion (turn-and-talk, whole class, and so on) to develop and reinforce critical and creative thinking skills.

Routine Problems

These are problems in which the way to a solution is generally straightforward. The solution usually involves one or two arithmetic operations.

Problem Types

Efforts are made to offer a variety of types of routine problems for students to solve in ***Hands-On Problem Solving***. As such, those problems focusing on number concepts include the following operations and problem types:

- Addition and subtraction: Beginning unknown, middle unknown, and end result unknown
- Multiplication: Product unknown
- Division: Quotitive and partitive division

These problem types are described in detail in the Implementation of Routine Problems section (see page 26).

Non-Routine Problems

These problems are more challenging for students. Upon first reading, the path to a solution is not immediately evident. Students draw on a bank of strategies (teacher-presented and student-developed) to solve the problem. Possible strategies include the following:

1. Act it out/use materials.
2. Draw a picture/diagram.
3. Look for a pattern.
4. Use logical reasoning.
5. Guess and check.
6. Make an organized list.
7. Make a table.
8. Work backwards.
9. Use an equation.
10. Use simpler numbers.

Some non-routine problem-solving strategies are more appropriate for use at specific grades than others. The chart below provides details for when each strategy is addressed in the ***Hands-On Problem-Solving*** program:

Descriptions of these strategies are provided in detail in the Implementation of Non-Routine Problems section (see page 120).

Strategy	Grade 1	Grade 2	Grade 3	Grade 4	Grade 5	Grade 6	Grade 7	Grade 8
Act it out/use materials	✓	✓	✓	✓	✓	✓	✓	✓
Draw a picture/diagram	✓	✓	✓	✓	✓	✓	✓	✓
Look for a pattern	✓	✓	✓	✓	✓	✓	✓	✓
Use logical reasoning	✓	✓	✓	✓	✓	✓	✓	✓
Guess and check		✓	✓	✓	✓	✓	✓	✓
Make an organized list		✓	✓	✓	✓	✓	✓	✓
Make a table			✓	✓	✓	✓	✓	✓
Work backwards					✓	✓	✓	✓
Use an equation					✓	✓	✓	✓
Use simpler numbers					✓	✓	✓	✓

Extended Exploration Problems

Extended exploration problems are meant to provide a thought-provoking challenge for students. These problems may present mathematical situations that are slightly beyond the grade-level curricular outcomes, may take the form of an investigation, or may require an extended period of time to solve. In all cases, students are encouraged to use their own strategies to arrive at a solution(s).

Extended problems are open ended, can be investigative in nature, and have multiple entry points to allow for differentiation. They often

- Have more than one solution/answer;
- Can be solved using a variety of strategies;
- Require students to gather their own data;
- Require creative and critical thinking;
- Require more/extended time to solve;
- Make connections to the real world.

Extended exploration problems support the other six “big idea” mathematical processes: communication, connections, mental math, estimation, reasoning, technology, and visualization. The engaging nature of these problems helps students develop perseverance.

Examples and procedures for extended exploration problems are described in detail in the Implementation of Extended Exploration Problems section (see page 224).

Implementing the Hands-On Problem-Solving Program

Hands-On Problem Solving is arranged in a format that makes it easy for teachers to plan and implement, with tasks that relate to specific outcomes/learning expectations established in Canadian curriculum documents.

Program Format

Problem-solving tasks are presented as daily mathematics activities and are organized according to the approximate number of weeks in the school year. As such, there are 40 weeks-worth of problem-solving tasks, consisting of

- 40 routine problems that focus on math topics including number, patterns, measurement, and geometry. These problems are identified as problems 1A through 40A;
- 40 non-routine problems that focus on specific strategies for the grade level. These problems are identified as problems 1B through 40B;
- 10 extended exploration problems that offer in depth, real-life contexts as the basis for problem solving. These problems are identified as problems 1C through 10C.

Planning your Year of Problem Solving

The three types of problems (routine, non-routine, and extended explorations) are presented in three separate sections of this book, each with its own detailed introduction on implementation. However, it is essential that students focus on all three types of problems throughout the school year. Therefore, it is recommended that teachers do one routine and one non-routine routine problem with students each week, and one extended exploration each month.

In the following section of *Hands-On Problem Solving* a correlation chart identifies the math concepts presented in each lesson of the book. Teachers can refer to this chart to plan problem-solving activities that correspond with other math activities occurring in the classroom. For example, if students are focusing on 2-D shapes in math, the correlation chart will show which problems herein connect to that topic.

Curricular Connections

Efforts have been made to correlate ***Hands-On Problem Solving*** problems with other curricular areas, such as language arts, science, and social studies. For example, some problems connect specifically to a science or social studies topic or to a general area of emphasis such as social justice. As teachers become familiar with the problems, they will find opportunities to connect these problems to specific units or topics of study.

Supporting Literacy During Problem Solving

It is important that all students, regardless of reading ability, have the opportunity to participate and succeed in problem solving. As such, some will require additional supports to read and understand the problems presented. To help support students' literacy skills, consider the following options:

- Read the problem aloud, and have students follow along.
- Read the problem as a class.
- Have students work with partners or in small groups to read and discuss the problem.
- Introduce, discuss, and review related math vocabulary, and display pictorial representations in the classroom (for example, display labelled illustrations of triangles, squares, and rectangles during a lesson in which students must draw on their knowledge of 2-D shapes).

The Questioning Process

During the problem-solving process, it is important for teachers and students to pose questions and to consider various strategies for solving the problem. To encourage these processes, blackline masters of guiding questions have been included for teacher and student use (see page 10). These two templates

(one for teacher use and the other for student use) provide suggested questions that can be asked during the problem-solving process.

The blackline masters can be photocopied onto sturdy tag board and laminated for long-term use. Teachers may choose to use these resources during lessons, as they support students in their problem solving. Students can glue their cards into problem-solving file folders or notebooks, or the cards can be placed on desks or tables for use during problem-solving activities.

Additional Resources

For some problem-solving tasks, students might use strategies requiring specific materials, such as hundred charts, number lines, graph paper, dot paper, and so on. These materials can be found in the Appendix at the back of the ***Hands-On Problem Solving*** book (see page 261); teachers are encouraged to photocopy these resources and distribute them to students as needed.

A Note About Pennies

The Government of Canada, in its 2012 Budget, announced its intention to withdraw the Canadian penny from circulation; as of fall 2012 the Royal Canadian Mint will no longer distribute pennies. However, the Government of Canada has also indicated that

- The penny will remain Canada's smallest unit for pricing of goods and services.
- The penny will retain its value indefinitely, and consumers can continue to use it in payments for goods and services.

Government of Canada Budget 2012 – Eliminating the Penny <www.budget.gc.ca/2012/themes/theme2-eng.html>

Pennies are included in some problems in the ***Hands-On Problem Solving*** program. The rationale for this is that using pennies in a problem-solving context

- Supports counting skills;
- Builds familiarity with money;
- Lends itself to grouping and place-value structure of base ten;
- Prepares students for global citizenship. Many monetary systems still include a penny or other coin with a value of 1;
- Can extend to opportunities to explore other Canadian coins that are in circulation but may not be used on a regular basis (for example the 50 cent coin).

Mathematics Correlation

The ***Hands-On Problem-Solving*** series has been designed to complement the mathematics program at any given grade level, with lessons (problems) that address the various mathematics topics and concepts focused on in grade 4.

The following chart indicates how lessons in the program connect to these math topics and concepts.

These correlations are based on an in-depth review of mathematics curriculum documents from across Canada, including the Western/Northern Canadian Protocol (WNCP), Ontario, and Atlantic Canada.

Grade 4 Correlation Chart

MATHEMATICS TOPIC	LESSON (PROBLEM) NUMBER
Number	
Representing numbers to 10 000	4A, 2B, 14B, 27B, 1C
Comparing and ordering numbers to 10 000	4A, 27B, 1C
Operations	
Addition	1A, 2A, 3A, 4A, 6A, 8A, 12A, 13A, 17A, 19A, 26A, 34A, 3B, 4B, 8B, 9B, 18B, 21B, 22B, 24B, 28B, 34B, 36B, 37B, 1C, 2C, 4C, 5C, 6C, 7C, 8C, 9C, 10C
Subtraction	2A, 3A, 6A, 9A, 12A, 13A, 19A, 3B, 4B, 30B, 2C, 6C, 8C, 9C
Multiplication	5A, 8A, 9A, 15A, 16A, 17A, 22A, 25A, 8B, 11B, 13B, 18B, 20B, 21B, 22B, 36B, 37B, 38B, 40B, 2C, 3C, 4C, 5C, 6C, 7C, 9C, 10C
Division	5A, 7A, 23A, 24A, 28A, 31A, 32A, 35A, 37A, 11B, 26B, 2C, 3C, 10C
Estimating sums and differences	16A, 17A, 2C, 10C
Describing and representing fractions	7A, 26A, 27A, 23B, 3B, 9C
Comparing and ordering fractions	20A, 5B, 25B
Relating fractions to decimals	10A, 21A
Describing and representing decimals	9A, 25B
Addition of decimals	10A, 18A, 15B, 16A, 19B, 28B, 31B, 5C, 10C
Subtraction of decimals	10A, 11A, 14A, 18A, 31B, 5C, 10C
Mental math	5A, 17A, 29A, 7B, 11B, 2C, 4C, 5C, 6C, 7C, 9C
Money	10A, 16A, 18A, 21A, 29A, 28B, 31B, 5C, 10C

Patterns and Relations	
Increasing patterns on a table/chart	29A, 7B, 9B, 17B, 28B, 40B, 6C
Decreasing patterns on a table/chart	8B
Using symbols to represent unknown numbers	2A, 11A, 10B, 13B, 29B
Measurement	
Length	6A, 11A, 13A, 14A, 17A, 37A, 4B, 15B, 22B, 36B, 38B, 4C, 9C
Perimeter	37A, 22B, 4C
Area	37A, 26B, 38B, 4C
Measurement of time	8A, 15A, 38A, 39B, 2C
Analogue clock	39A, 6C
24-hour clock	36A, 40A, 3C
Calendar/dates	38A, 40A, 16B
Geometry	
2-D shapes	31A, 32A, 33A, 35B, 36B, 38B, 7C
3-D objects	34A, 35A, 7C
Symmetry	33A, 7C
Data Analysis	
Pictograph	30A, 5C
Graphs	3A, 6A, 8A, 11A, 26A, 30A
Many-to-one correspondence	5C
Representing and interpreting data on charts/tables	29A, 7B, 8B, 9B, 17B, 28B, 40B, 3C, 6C

A decorative crosshair consisting of a vertical line and a horizontal line intersecting at the origin.

Routine Problems

1A Mad About Marbles

Math Topic

Number

Math Concept

Three-digit addition

Problem Type

Addition: Middle unknown ($a + ? = c$)

Problem

Jade and Max are entered in the National Marble Competition.

Jade has 375 marbles in her bag.

Max has a bag of marbles too.

Together they have 523 marbles.

How many marbles does Max have?

Background Information for Teachers

The first routine problem is a review of grade 3 skills in three-digit addition, offering an opportunity to determine students' background knowledge and entering skills. To scaffold the problem, present the following number sentences:

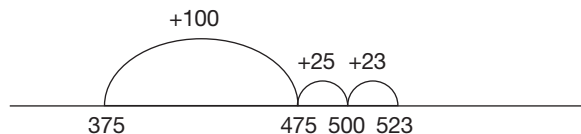
- $27 + 30 = ?$
- $75 + ? = 100$
- $143 + 259 = ?$
- $601 + ? = 725$

Have students share their strategies for calculating these number sentences, and observe them as they approach each task.

Students may use a variety of strategies to solve this problem, such as the following:

- Use manipulatives, such as base-ten materials and place-value charts to build the problem
- Draw a picture, such as base-ten materials

- Use an empty number line, beginning at 375 and jumping to 523, as in the following illustration:



- Write a number sentence: $375 + ? = 523$



Think

Provide time for students to read, think, and formulate ideas about the problem.



Talk

Discuss the problem with students. Ask:

- What do you need to find out? (how many marbles Max has)
- What is important information in the problem? (Highlight the important information.)
- What is not important? (Underline the unimportant information.)
- Can you name the answer? (marbles)
- In what ways can the problem be solved?
- What materials can you use to solve the problem?
- What strategies can you use to solve the problem?

Have students share their ideas about materials and strategies they might use to solve the problem. Encourage students to ask questions. Discuss the problem as a class, in small groups, or in pairs. Encourage communication through the use of rich, probing questions and meaningful conversations with and among students.



Solve

$$375 + 148 = 523$$

Max has 148 marbles.

1A

Share



Have students share their strategies and solutions.

Extend

To extend the preceding problem for students, have them record the answer in a complete sentence, using all words and no numerals.

Date: _____

Sample Pages

Name: _____

Mad About Marbles

Jade and Max are entered in the National Marble Competition.

Jade has 375 marbles in her bag.

Max has a bag of marbles too.

Together they have 523 marbles.

How many marbles does Max have?



Think



Talk



Solve



Share

2A Gathering Acorns

Math Topics

- Number
- Variables and equations

Math Concepts

- Three-digit addition
- Three-digit subtraction
- Using symbols to represent an unknown number

Problem Type

Addition: Beginning unknown ($? + b = c$)

Problem

The grade four class is making nature collages.

Jacee gathers some acorns for the project.

Miranda gathers 125 acorns.

Together they gather 403 acorns.

How many acorns does Jacee gather?

Background Information for Teachers

This problem may be solved with both addition and subtraction, depending on students' understanding of the relationship between the two operations.

Students may use a variety of strategies to solve this problem, such as the following:

- Use manipulatives, such as base-ten materials
- Draw a picture
- Use an empty number line
- Write a number sentence:
 $? + 125 = 403$ or $403 - 125 = ?$

This problem presents an excellent opportunity to introduce students to the use of symbols to represent an unknown number in an equation. As students write number sentences for this

problem, discuss the ways that symbols can be used for the unknown number, for example:

$$\square + 125 = 403$$

$$\square + 125 = 403$$

$$\triangle + 125 = 403$$

Think



Provide time for students to read, think, and formulate ideas about the problem.

Talk



Discuss the problem with students. Ask:

- What do you need to find out? (how many acorns Jacee gathers)
- What is important information in the problem? (Highlight the important information.)
- What is not important? (Underline the unimportant information.)
- Can you name the answer? (acorns)
- In what ways can the problem be solved?
- What materials can you use to solve the problem?
- What strategies can you use to solve the problem?

Discuss the problem as a class, in small groups, or in pairs. Encourage communication through the use of rich, probing questions and meaningful conversations with and among students. Have students share their ideas about materials and strategies they might use to solve the problem. Encourage students to ask questions.

Solve



$$278 + 125 = 403 \text{ or } 403 - 125 = 278$$

Jacee gathers 278 acorns.

Share



Have students share their strategies and solutions.

2A

Extend

Present the following extension problem to students:

Who gathers more acorns, Jacee or Miranda?

How many more acorns does she gather?

Date: _____

Sample Pages

Name: _____

Gathering Acorns

The grade four class is making nature collages.

Jacee gathers some acorns for the project.

Miranda gathers 125 acorns.

Together they gather 403 acorns.

How many acorns does Jacee gather?



Think



Talk



Solve



Share