

NUMBER OPERATIONS
GRADE 3
ONTARIO EDITION

hands-on
mathematics

Project Editor

Jennifer E. Lawson

Senior Author

Dianne Soltess

Mathematics Consultant

Meagan Mutchmor

Unit Writers

Patricia Ashton

Joni Bowman

Gail Ruta Fontaine

Betty Johns

Cathy Haggart

Kara Kolson

Suzanne Mole



PORTAGE & MAIN PRESS

Winnipeg • Manitoba • Canada

© 2007 Jennifer Lawson

From *Hands-On Mathematics: Grade 3*, © 2006

Portage & Main Press acknowledges the financial support of the Government of Canada through the Book Publishing Industry Development Program (BPIDP) for our publishing activities.

All rights reserved. With the exceptions of student activity sheets and evaluation forms individually marked for reproduction, no part of this publication may be reproduced or transmitted in any form or by any means – graphic, electronic, or mechanical – without the prior written permission of the publisher.

Series Editor:	Leslie Malkin
Book and Cover Design:	Relish Design Ltd.
Illustrations:	Jess Dixon
Senior Author:	Dianne Soltess
Mathematics Consultant:	Meagan Mutchmor

Number Operations

Grade 3

Ontario edition

Printed and bound in Canada by Prolific Group

ISBN 978-1-55379-101-0



PORTAGE & MAIN PRESS

100-318 McDermot Avenue

Winnipeg, Manitoba, Canada R3A 0A2

Email: books@portageandmainpress.com

Tel: 204-987-3500

Toll Free: 1-800-667-9673

Fax: 1-866-734-8477

Contents

Introduction to <i>Hands-On Mathematics</i>	1	15 Choosing a Method for Solving Problems	111
Program Introduction	1	16 Addition and Subtraction with Money	114
Program Principles	1	17 Multiplication	116
The Big Ideas of Mathematics	1	18 Commutative Property of Multiplication	123
<i>Ontario Curriculum for Mathematics (2005)</i>		19 Multiplying by 1 and by 0	130
Learning Expectations	5	20 Combination-Multiplication Problems	134
Program Implementation	7	21 Multiplication Facts	136
Classroom Environment	8	22 Division	141
Timelines	8	23 Missing Factors	150
Classroom Management	8	24 The Inverse Relationship between Multiplication and Division	155
Planning Guidelines	9	25 Multiplication and Division Facts	162
Assessment	12	Problem-Solving Black Line Master: Number Operations	166
The <i>Hands-On Mathematics</i> Assessment Plan	12	References for Teachers	174
Websites	27		
Number Operations	31		
Books for Children	32		
Introduction	34		
1 Addition and Subtraction Facts to 18	35		
2 More Addition and Subtraction Facts	39		
3 One- and Two-Digit Addition and Subtraction	47		
4 Addition and Subtraction with a Calculator	53		
5 Addition of Hundreds	55		
6 Compatible Numbers	61		
7 Estimating Sums and Differences by Rounding to Tens	69		
8 Addition with Three-Digit Numbers	75		
9 More Addition with Three-Digit Numbers	78		
10 Solving Multiple-Step Problems	84		
11 Subtraction with Three-Digit Numbers	85		
12 More Subtraction with Three-Digit Numbers	87		
13 Making Purchases and Change to Ten Dollars	94		
14 Representing a Given Dollar Value in Different Ways	107		

Introduction

The goal of the module, *Number Operations* is to enhance students' computational fluency with addition, subtraction, multiplication, and division. In keeping with this goal, the activities in this module promote the use of various methods of computing.

The activities involving addition and subtraction focus on recalling basic number facts for these operations and on computing with three-digit numbers. They also highlight student-created algorithms, the development of estimation and mental-math skills, and the appropriate use of calculators. Of particular significance is the emphasis on student-created algorithms. Unlike traditional algorithms, student-generated algorithms give students additional insight into place-value concepts and the relationships between numbers.

It is important to note that number-operation questions are primarily presented in a horizontal format, which encourages the use of mental math and student-created algorithms. A vertical format implies the use of the standard algorithm, which inhibits students' number-sense abilities and flexible-thinking strategies.

The activities involving multiplication and division focus on basic number facts for these operations. They also include the development of operational properties such as the relationship between multiplication and division. These properties extend students' understanding of the operations and provide them with important strategies for learning the basic facts.

Many of the activities in this module involve a problem-solving approach to the teaching of mathematics, which encourages students to explore new ideas and to make sense of mathematical concepts in ways that are meaningful to them. It also encourages students to share their findings and justify their conclusions. It is a powerful technique that

helps students develop their abilities to solve problems, to communicate, and to reason mathematically.

Several lessons in this module include a section called "Next Steps," which guides teachers through a subsequent sequence of activities to carry out with students, following developmentally from the main activities. For example, in lesson 7, students are introduced to the addition strategy of rounding three-digit addends to the nearest hundred in order to quickly and easily find the sum. Once students master this technique, the next step is to repeat the rounding/estimation activity as a subtraction strategy for finding the difference between three-digit numbers.

Mathematics Vocabulary

Continue to use your classroom mathematics word wall to display new vocabulary as it is introduced. Throughout this module, teachers should use, and encourage students to use, vocabulary such as: *bridge to ten*, *compatible number*, *product*, *factor*, *times*, *divide*, *divisible*, *multiple*, *odd*, and *even*. Use, and encourage students to use, this vocabulary both orally and in writing, and continue to review all vocabulary previously introduced.

Depending on your students' writing skills, also consider having them begin mathematics logbooks for recording:

- new math vocabulary
- mental-math strategies
- problem-solving strategies
- graphic organizers

Note: For ideas on using mental math strategies, see the module, *Mental Math Activities: Grades 1-3*.

3

One- and Two-Digit Addition and Subtraction

Materials

- blank ten frames (templates included. Photocopy at least five blank ten frames onto overhead transparencies.) (6.3.1)
- pennies
- overhead projector
- overhead transparencies
- overhead markers
- scrap paper
- pencils
- addition and subtraction cards (included. Photocopy one set of cards for each pair of students. Mount cards onto sturdy tagboard, and cut out.) (6.3.3)

Activity: Part One

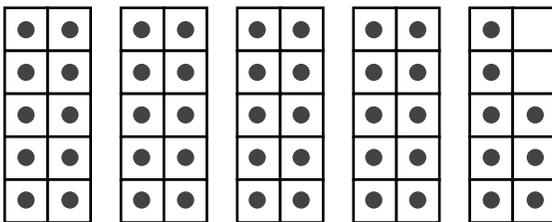
Present the following problem to students.

Mark has 48¢ in his pocket. His sister gives him 5¢ more. How much money does Mark have now?

Tell students that you will now use ten frames to solve this problem. Ask:

- How can we use pennies with the ten frames to show 48¢?

Place five blank ten frames onto the overhead, and use pennies to show the 48¢ that Mark originally had in his pocket, as in the following diagram.



Now, have students determine how to use the ten frames to add the additional 5¢ Mark's sister gave to him. Place five more pennies onto the overhead, beside the ten frames. Then, point to

the ten frame with only eight pennies, and ask students:

- How many more pennies do we need to add to the eight pennies to equal ten pennies and fill the frame?

Move two pennies from the group of five pennies beside the ten frames onto the ten frame with eight pennies, to fill the frame. Ask:

- What is 48 plus 2?
- How many pennies are left over from the group of five pennies that was beside the ten frames? (3)
- What is 50 plus 3?

Tell students that $48 + 5 = 53$, since $48 + 2 = 50$ and 3 more is 53. Explain that students found the sum of $48 + 5$ by *bridging to ten*.

Repeat the procedure for new problems such as

- $28 + 6 = \underline{\quad}$
- $7 + 8 = \underline{\quad}$
- $49 + 7 = \underline{\quad}$

Distribute Activity Sheet A (6.3.2), and have students make each problem easier to solve by bridging to ten. Then, have students find the sum for each problem.

Activity Sheet A

Directions to students:

Make each problem easier to solve by bridging to ten. Then, find the sum (6.3.2).

Activity: Part Two

Record the following two problems on the overhead:

$$27 + 8 = \underline{\quad} \qquad 30 + 5 = \underline{\quad}$$

Distribute scrap paper and pencils, and have students find the answer to each problem.

3

Ask:

- What strategy did you use to solve each problem?
- Did you find a way to simplify each problem?

Have students share the strategies they used to solve the problems. Stress that any strategy is valid if it enables you to answer a problem.

Using the two previous problems as examples, demonstrate, or have a student demonstrate, how to make a problem easier to solve by using the bridge-to-ten strategy. For example:

The problem $30 + 5 = \underline{\quad}$ was fairly easy to solve because I simply added the ones (5) to the tens (30).

To solve the problem $27 + 8 = \underline{\quad}$, I split up the 8 into 3 and 5 and bridged to 30. The problem then became $30 + 5 = 35$.

Now, record the following sets of problems on the overhead:

$$56 + 7 = \underline{\quad} \quad 60 + 3 = \underline{\quad}$$

$$38 + 5 = \underline{\quad} \quad 40 + 3 = \underline{\quad}$$

$$76 + 6 = \underline{\quad} \quad 80 + 2 = \underline{\quad}$$

Have students find the answer(s) to each set of problems. Ask:

- What strategy did you use to solve each problem?
- Did you find a way to simplify any of the problems? Which problem(s), and how did you simplify it (them)?

Have students share the strategies they used to solve the problems.

Activity: Part Three

Divide the class into pairs of students, and give each pair a set of addition and subtraction cards (included, 6.3.3). Have students in each pair sort

their cards into two sets: easier to solve and harder to solve.

When students finish sorting the cards, have them share their results and explain their reasoning.

Problem Solving

Note: Orally present the following story problems, and have students solve them mentally, encouraging them to use the bridge-to-ten strategy.

- Jake found 7 seashells on the beach. He took them home and added them to the 28 seashells he collected last week. How many seashells does Jake have now?
- There are 36 horses in the corral. Dario opened the gate and let in 8 more horses. How many horses are in the corral now?
- Sophie had 86¢. Her brother Ryan found 6¢, and he gave it to Sophie. How much money does Sophie have now?
- Forty-seven third-grade students go to summer camp. Nine fourth-grade students also go to camp. Altogether, how many third- and fourth-grade students go to summer camp?
- Mel is 18 years old. Her brother is 6 years older than she is. How old is Mel's brother?
- Bill is using centimetre blocks to build a tower. On Monday, the tower was 38-centimetres high. On Tuesday, he added another 5 centimetres to the height of his tower. What is the total height of Bill's tower now?

Note: Reproducible masters for these problems can be found on pages 166 and 167.

3

Extensions

- Add the term *bridge to ten* to your classroom math word wall.
- Introduce students to the bridge-to-ten strategy for subtraction. For example, to find the difference between 38 and 44 ($44 - 38 =$):
 - think $38 + 2 = 40$, and 4 more equals 44
 - $2 + 4$ is 6
 - $44 - 38 = 6$

Blank Ten Frames

Bridge to Ten

Example: $26 + 8 =$

$26 + 4 = 30$ and 4 more is 34.

Problem	Bridge-to-Ten Strategy	
$19 + 6 =$ _____	_____ + _____ = _____ and _____ more is	<input type="text"/>
$49 + 9 =$ _____	_____ + _____ = _____ and _____ more is	<input type="text"/>
$35 + 8 =$ _____	_____ + _____ = _____ and _____ more is	<input type="text"/>
$86 + 5 =$ _____	_____ + _____ = _____ and _____ more is	<input type="text"/>
$77 + 4 =$ _____	_____ + _____ = _____ and _____ more is	<input type="text"/>
$54 + 8 =$ _____	_____ + _____ = _____ and _____ more is	<input type="text"/>
$28 + 7 =$ _____	_____ + _____ = _____ and _____ more is	<input type="text"/>
$15 + 8 =$ _____	_____ + _____ = _____ and _____ more is	<input type="text"/>
$47 + 6 =$ _____	_____ + _____ = _____ and _____ more is	<input type="text"/>
$36 + 9 =$ _____	_____ + _____ = _____ and _____ more is	<input type="text"/>

Addition and Subtraction Cards

$29 + 5 =$	$88 + 8 =$	$50 + 8 =$	$46 + 8 =$
$38 + 6 =$	$30 + 3 =$	$40 + 2 =$	$69 + 4 =$
$70 + 5 =$	$40 + 9 =$	$75 + 8 =$	$80 + 6 =$
$87 + 7 =$	$20 + 7 =$	$10 + 9 =$	$57 + 5 =$
$60 + 4 =$	$86 + 9 =$	$90 + 1 =$	$36 + 9 =$